

LINE: Queueing Analysis Algorithms

A Primer – MATLAB Edition

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Chapter 1

Introduction

1.1 What is LINE?

LINE is an open-source software package for the analysis of queueing models by analytical methods and simulation. It is developed by the QORE lab at Imperial College London and distributed under the BSD-3 license. The package solves single queueing systems (M/M/1, M/M/k, M/G/1, ...), open and closed queueing networks, layered queueing networks, and models embedded in random environments. Models are solved either by LINE's native algorithms or through external solvers such as JMT, LQNS, MAMSolver, Q-MAM, SMCSolver, and BuTools.

This document is a short *primer*: a self-contained tour of the core modelling concepts and solvers, using a handful of runnable examples. It is produced in three editions that share the same text but show the code in MATLAB. It deliberately shows one worked example per topic; for many more examples, additional features, and the other language editions, see the full LINE manual on the LINE website.

1.2 Available editions

LINE ships in several interoperable implementations that expose the same modelling concepts:

Edition	Requirements	Notes
MATLAB	MATLAB	Original, most mature surface
Java (JAR)	Java SE 8+	Canonical implementation, <code>jline.jar</code>
Kotlin	Java SE 8+	Calls <code>jline.jar</code> unchanged (uses the Java API)
Python native	Python 3.11+	Pure-Python algorithms
Python wrapper	Python 3.11+, Java 8+	Calls <code>jline.jar</code> via JPYpe (fastest)

The MATLAB edition requires a MATLAB installation and adds the `line/` folder to the path; no compilation is needed.

1.3 Obtaining and installing LINE

Download the latest release, unzip it, and run `lineStart` from the `line/` folder to add LINE to the MATLAB path. The latest releases and source are available from <http://line-solver.sf.net>.

1.4 License and acknowledgement

LINE is released under the BSD-3 license and is maintained by the QORE lab. If you use LINE in academic work, please cite the package and the relevant method papers. LINE has been partially funded by the European Commission grants FP7-318484 (MODAClouds), H2020-644869 (DICE), H2020-825040 (RADON), and the EPSRC grant EP/M009211/1 (OptiMAM).

Chapter 2

Getting started

2.1 A first model: the M/M/1 queue

A LINE script has four conceptual blocks: (1) create the *nodes* (stations), (2) declare the *job classes*, (3) assign *arrival* and *service* processes, and (4) specify the *topology* (routing). The model is then handed to a *solver*. The following script builds and solves an M/M/1 queue with arrival rate $\lambda = 1$ and service rate $\mu = 2$; theory gives utilization $\rho = \lambda/\mu = 0.5$ and mean response time $1/(\mu - \lambda) = 1$ s.

```
model = Network('M/M/1');
% Block 1: nodes
source = Source(model, 'Source');
queue = Queue(model, 'Queue', SchedStrategy.FCFS);
sink = Sink(model, 'Sink');
% Block 2: classes
jobclass = OpenClass(model, 'Class1');
% Block 3: arrival and service processes
source.setArrival(jobclass, Exp(1)); % lambda = 1
queue.setService(jobclass, Exp(2)); % mu = 2
% Block 4: topology
model.link(Network.serialRouting(source, queue, sink));
% Solve
AvgTable = MVA(model).avgTable()
```

2.2 Reading the results

Every average-metric solver returns a table with one row per (station, class) pair. The main columns are:

Column	Meaning
QLen	mean number of jobs at the station (queue length)
Util	utilization (busy fraction / mean number in service)
RespT	mean response time per visit
ResidT	mean residence time (response time weighted by visits)
ArvR	mean arrival rate
Tput	mean throughput

Individual rows are selected as follows:

```
ARow = AvgTable(queue, jobclass) % by object
QRows = AvgTable.filterBy(queue) % all rows for a node
```

Stochastic solvers accept a seed for reproducibility and a samples budget, e.g. `JMT(model, 'seed', 23000, 'sa`. Verbosity is controlled globally through `GlobalConstants`.

Chapter 3

Network models

3.1 Model-construction workflow

The `Network` object is the container for all model elements. Elements register themselves with the model passed to their constructor. The four-block workflow of Chapter 2 scales to arbitrary networks; only the number of nodes, classes and routes grows.

3.2 Nodes, scheduling and classes

Node	Role
Source / Sink	external arrival / departure (open classes)
Queue	queueing station with a scheduling discipline
Delay	infinite-server (pure think time / delay)
Router	pure routing / load-balancing node
ClassSwitch	changes the class of transiting jobs
Cache	caching node (hit/miss with a replacement policy)
Fork / Join	fork-join parallelism
Place / Transition	stochastic Petri-net elements

The scheduling discipline is passed to the `Queue` constructor as a `SchedStrategy` value: FCFS (first-come first-served), PS (processor sharing), INF (infinite server), LCFS, SIRO (random order), HOL (head-of-line priority), SEPT/LEPT, and DPS/GPS. A queue's server count is set with `setNumberOfServers`. Two class kinds exist: `OpenClass` jobs enter at a `Source` and leave at a `Sink`; `ClosedClass` jobs circulate among a fixed population with a designated reference station. Open and closed classes may coexist in a mixed model.

3.3 Distributions

Arrival and service processes are distribution objects: `Exp` (exponential), `Erlang`, `HyperExp`, `Cox2/APH` (phase-type), `Det` (deterministic), `Uniform`, `Gamma`, `Pareto`, `Lognormal`, `MAP/MMPP2` (Markovian arrivals), and `Replayer` (empirical trace). Non-exponential timing is handled by phase-type expansion or by fitting: `Erlang.fitMeanAndSCV(m, scv)` matches a target mean and squared coefficient of variation.

3.4 A closed-network example

A machine-repairman model: three machines alternate between a working (infinite-server) delay and a two-server repair queue, solved exactly with the CTMC solver.

```
model = Network('MRP');
delay = Delay(model, 'WorkingState');
queue = Queue(model, 'RepairQueue', SchedStrategy.FCFS);
queue.setNumberOfServers(2);
cclass = ClosedClass(model, 'Machines', 3, delay); % N=3, ref=delay
delay.setService(cclass, Exp(0.5));
queue.setService(cclass, Exp(4.0));
model.link(Network.serialRouting(delay, queue));
ctmcAvgTable = CTMC(model).avgTable()
```

The reference station (here `delay`) passed to the closed-class constructor marks where a job is considered to have completed a cycle.

3.5 Routing and advanced features

Serial chains use `serialRouting` inside `link`; point-to-point links are added with `model.addLink(a,b)`, and per-node behaviour is set with `setRouting` using a `RoutingStrategy` such as `RAND`, `RROBIN` (round robin), `PROB` (probabilistic), or `JSQ` (join shortest queue). Class-dependent routing uses a routing matrix obtained from the model and populated per class. LINE also supports finite-capacity regions, reward models, caches with replacement policies, class switching, and stochastic Petri nets; these are covered in the full manual.

Chapter 4

Analysis and solvers

4.1 Performance metrics

The primary analysis is steady-state average performance, obtained with the average-table method (all station/class metrics) or a finer-grained average method returning the metric matrices directly. System-level aggregates and, for Markovian models, the underlying state space and generator are also available (e.g. from the CTMC solver), together with transient averages and response-time distributions.

4.2 Solvers

A solver takes a model and options and returns metrics; all are invoked uniformly as *Solver(model, options)* followed by the average-table method.

Solver	Method	Best for
CTMC	continuous-time Markov chain	exact, small state spaces
MVA	mean value analysis	product-form open/closed, fast
NC	normalizing constant	large closed populations
FLD	fluid / mean-field ODE	large populations, transient
SSA	stochastic simulation (native)	general, any feature
MAM	matrix-analytic methods	MAP/PH open models
JMT	external simulation (JMT)	validation, general
LN	layered network solver	layered models (Ch. 5)
LQNS	external LQN solver	layered models
ENV	random-environment blending	environment models (Ch. 6)

As a rule of thumb, use CTMC for small exact models; MVA/NC for product-form networks at scale; FLD for very large populations or transients; MAM for Markovian-arrival or phase-type open models; and SSA/JMT when a feature is not supported analytically. Running two solvers and comparing is good practice, as every solver consumes the same model object unchanged.

Chapter 5

Layered queueing networks

A `LayeredNetwork` (LQN) captures software contention on top of hardware contention. Its elements are *processors* (hardware servers), *tasks* (software resources with a multiplicity), *entries* (the service interfaces a task offers), and *activities* (units of work that issue synchronous or asynchronous calls to other entries). The example below is a two-tier client–server application.

```
model = LayeredNetwork('ClientDBSystem');
P1 = Processor(model, 'ClientProcessor', 1, SchedStrategy.PS);
P2 = Processor(model, 'DBProcessor', 1, SchedStrategy.PS);
T1 = Task(model, 'ClientTask', 10, SchedStrategy.REF).on(P1);
T1.setThinkTime(Exp.fitMean(5.0));
T2 = Task(model, 'DBTask', Inf, SchedStrategy.INF).on(P2);
E1 = Entry(model, 'ClientEntry').on(T1);
E2 = Entry(model, 'DBEntry').on(T2);
A1 = Activity(model, 'ClientActivity', Exp.fitMean(1.0)).on(T1);
A1.boundsTo(E1).synchCall(E2, 2.5); % 2.5 DB calls per request
A2 = Activity(model, 'DBActivity', Exp.fitMean(0.8)).on(T2);
A2.boundsTo(E2).repliesTo(E2);
AvgTable = LN(model, @(m) MVA(m)).avgTable()
```

The native LN solver decomposes the model into layers and applies a supplied per-layer solver (here MVA); the external LQNS solver may be used when available.

Chapter 6

Random environments

A random environment models a system whose parameters change according to an underlying stochastic process. Each *stage* is a complete network with its own parameters, and stage transitions follow specified distributions. The example alternates a closed model's server between a fast mode ($\mu = 4$) and a slow mode ($\mu = 1$); we assume a base closed model `baseModel` has already been built.

```
env = Environment('ServerModes');
fastModel = baseModel.copy();
fastModel.getNodeByName('Server').setService(fastModel.classes{1}, Exp(4.0));
env.addStage('Fast', 'operational', fastModel);
slowModel = baseModel.copy();
slowModel.getNodeByName('Server').setService(slowModel.classes{1}, Exp(1.0));
env.addStage('Slow', 'degraded', slowModel);
env.addTransition('Fast', 'Slow', Exp(0.5));
env.addTransition('Slow', 'Fast', Exp(1.0));
envAvgTable = ENV(env, @(m) FLD(m)).getAvgTable()
```

The ENV meta-solver takes a factory that produces an inner solver for each stage and returns metrics averaged over the stationary distribution of the environment.

Chapter 7

Further resources

The `line-cli.py` script solves models without writing code, reading JMT's JSIMG and LQNS's LQNX formats and printing tables, JSON, or CSV:

```
python line-cli.py solve model.jsimg --solver mva
python line-cli.py list solvers
```

LINE is also available as a Model Context Protocol (MCP) server, letting LLM tools such as Claude Code build and solve models through natural language (`pip install line-solver`). The complete references are the MATLAB, Java/Kotlin, and Python manuals with their Doxygen, Javadoc, and Sphinx API references, plus the MCP getting-started guide, all linked from <http://line-solver.sf.net>.

For many more worked examples – additional queueing systems, layered and mixed networks, transient and distribution analysis, inference, and optimization – consult the full LINE manual for your language, which expands every topic in this primer in greater depth.